Worksheet 2: Friday 1/24

Exercises:

3

 $(-\infty,1) \cup (2,\infty)$ $(-\infty, 3)\nu(3, \infty)$

(-~,-4)~(3,~

- 1. Consider the functions f(x) = 2x + 1 and $g(x) = x^2 + 2$ defined on [-2, 2]:
 - (a) What is f(1)? What is g(0)? 3/2
 - (b) What is the range of f? What is the range of g? [-3, 5]

 - (d) Is f even, odd, both even and odd, or neither? Is g even, odd, both Neither, Even even and odd, or neither?

even and odd, or neither? (e) Where is f increasing/decreasing? Where is g increasing/decreasing? f increasing/f [-2,2] Consider the following functions: $f(x) = \frac{x^2 + 2x + 1}{p + 2x + 1}$ $f(x) = \frac{x^2 + 2x + 1}{p + 2x + 1}$

, [2,6]

 $f(x) = \frac{x^{2+2x+1}}{x^{-3}} = 2$

 $=> x^2 = -7$

2. Consider the following functions:

$$f(x) = \frac{x^2 + 2x + 1}{x - 3}$$
$$g(x) = \frac{x^2 - 2x - 3}{x - 3}$$

- (a) What is the domain of f? What is the domain of g? $(-\infty, 3) \cup (3, \infty)$
- (b) For which values of x do we have f(x) = 0 and g(x) = 0? $\chi = -1$ only
- (c) Sketch the graph of g(x).
- (d) Is there a value of x such that f(x) = 2? Justify your answer. $\mathcal{N}\mathcal{A}$
- 3. Find the domain of the following functions:

$$\frac{(-\infty,1)\nu(2,\infty)}{(-\infty,1)\nu(3,\infty)} = \frac{1}{\sqrt{x^2 - 3x + 2}}, \quad g(x) = \frac{1}{1 - \frac{1}{x - 2}}, \quad h(t) = \frac{\tan(t)}{1 + \sin(t)}$$

$$v(t) = \frac{t}{\sqrt[3]{t^2 - 1}}, \quad w(t) = \log(t^2 + t - 12)$$

$$\frac{1}{\sqrt{x^2 - 3x + 2}}, \quad w(t) = \log(t^2 + t - 12)$$

$$\frac{1}{\sqrt{x^2 - 3x + 2}}, \quad f(x) = x^2 - x + \frac{1}{4} \quad \begin{bmatrix} \mathcal{O}_1 & \mathcal{O}_1 \\ \mathcal{O}_1 & \mathcal{O}_1 \\ \mathcal{O}_1 & \mathcal{O}_2 \\ \mathcal{O}_1 & \mathcal{O}_2 \\ \mathcal{O}_2 & \mathcal{O}_2 \end{bmatrix}$$

$$f(x) = x^{2} - x + \frac{1}{4} [0, 9/4]$$

$$g(x) = \exp(-x) [2/2, e]$$

$$h(x) = x^{3} + x + 3 [1, 5]$$

- 5. (a) If the point (5,3) is on the graph of an even function, what other point (-5,3)must also be on the graph?
 - (b) If the point (5,3) is on the graph of an odd function, what other point (-5, -3) must also be on the graph?
- 6. (a) What is the parity of the product of two even functions? eVen

- (b) What is the parity of the product of two odd functions? eVeG
- (c) What is the parity of the product of an even function and an odd function?
- 7. Consider the following formulas, which ones can represent a function? Which ones cannot?

$$f(x) = x^{3} + \frac{1}{x^{3}}, \qquad g(x) = e^{x}$$

$$1 = x^{2} + y^{2}, \qquad 0 = y - \arcsin(x).$$

8. Write piecewise equations for functions that have the following graphs.

